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# The High Aromatic and Stable Clusters Li5B, Li6B+/- and Li7B: A Case of the [Phenomenological](https://www.researchgate.net/publication/221701949_The_High_Aromatic_and_Stable_Clusters_Li5B_Li6B-_and_Li7B_A_Case_of_the_Phenomenological_Shell_Model?enrichId=rgreq-4c53ef14-6d25-4e7f-9eea-b7dc800b5c4f&enrichSource=Y292ZXJQYWdlOzIyMTcwMTk0OTtBUzo5Nzc0MjcwMTQ2NTYxMkAxNDAwMzE1MDg0NjM4&el=1_x_3) Shell Model

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# The high stability of boron-doped lithium clusters Li $_5$ B, Li $_6$ B<sup>+/–</sup> and Li<sub>7</sub>B: A case of the phenomenological shell model

## Truong Ba Tai<sup>a</sup>, Minh Tho Nguyen<sup>a,b,</sup>\*

a Department of Chemistry, LMCC-Mathematical Modeling and Computational Science Center, Katholieke Universiteit Leuven, B-3001 Leuven, Belgium <sup>b</sup> Institute for Computational Science and Technology of HoChiMinh City, Thu Duc, HoChiMinh City, Viet Nam

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#### ABSTRACT

A quantum chemical investigation of the clusters  $Li_5B$ ,  $Li_6B^+$ ,  $Li_6B^-$  and  $Li_7B$  was performed using the DFT, MP2 and CCSD(T) methods. The high symmetry structures ( $C_{4v}$ ,  ${}^{1}A_1$ ), ( $O_{h}$ ,  ${}^{1}A_{1g}$ ) and ( $D_{5h}$ ,  ${}^{1}A'_1$ ) turnout to be the global minima for Li<sub>5</sub>B, Li<sub>6</sub>B<sup>+</sup> and Li<sub>7</sub>B, respectively. These clusters are predicted to be highly stable species with large vertical ionization energies, and large HOMO–LUMO gaps. Chemical bonding of clusters was probed using an electron localizability indicator (ELI) which indicates a large aromatic character. The high stability of these clusters can be accounted for by the phenomenological shell model.

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#### 1. Introduction

Binary clusters composed of two types of elements have greatly been attractive, in part due to their wide range of interesting structural and electronic features [1–3]. It has been well-known that addition of impurities leads to fundamental changes in the geometry, electronic structure, energetic properties and thermodynamic stability of the doped clusters as compared to the bare host. The phenomenological shell model (PSM) which was proposed by Knight et al. [4], has proved to be an effective tool to interpret the variation with size of the properties of metal clusters [5–7]. In the framework of this model, the valence electrons are assumed to freely itinerant in a simple mean-field potential that is formed by the nuclei of atoms. Accordingly, the high stability of a metal cluster is as achieved if its electronic shells or sub-shells are closed, and the number of valence electrons corresponds to a shell closing such as 2 (1S<sup>2</sup>), 8 (1S<sup>2</sup> 1P<sup>6</sup>), 20 (1S<sup>2</sup> 1P<sup>6</sup> 1D<sup>10</sup> 2S<sup>2</sup>), etc., that are called the magic numbers. However, this model was not successfully applied for some highly stable binary clusters of which number of valence electrons does not correspond to these magic numbers, such as  $K_8Zn$  [8], Na $_6Pb$  [9]. A modified phenomenological (Wood-Saxon) potential was introduced as an extended model to explain the behaviour of these cases [10–12]. In this model, the dopant induces a perturbation and the ordering of the single particle energy levels is changed either to  $(1S^2 1P^6 2S^2 1D^{10} 2P^6)$  if the impurity is more electronegative than the host atoms, or to  $(1S<sup>2</sup>$ 

 $1P^6$   $1D^{10}$   $2S^2$   $1F^{16}$   $2P^6$ ) if the central dopant is less electronegative than the host atoms.

Recently, lithium-based clusters have been investigated as a economic and simple model to approach the electronic structure of heavier metal clusters. A large number of the experimental and theoretical studies have been performed on pure lithium clusters [13,14] as well as on doped lithium clusters by many groups [15–17]. Theoretical investigations for boron-doped lithium clusters in both neutral and cationic states were performed by Nguyen et al.  $[18,19]$  and Li et al.  $[20,21]$ . Li et al. found that the neutral Li<sub>5</sub>B was pointed out to have a high stability in the series of  $Li<sub>n</sub>B$  clusters  $(n = 1-7)$ , whereas the cation  $Li<sub>6</sub>B<sup>+</sup>$  was found to have a high stability within the  $Li<sub>n</sub>B<sup>+</sup>$  cationic cluster state. These authors [20,21] showed that the stability patterns of these systems can be interpreted using the spherical jellium model (SJM) [22] in which a high stability is expected for the systems possessing 2, 8, 20, 34, etc., valence electrons (called as the magic numbers) that correspond to the electron configuration  $1s^2 1p^6 1d^{10} 2s^2 1f^{14}$ . The SJM has accounted for the high stability of the clusters containing eight valence electrons such as  $Li_5B$  and  $Li_6B^+$ , but it was failed for larger systems. The HOMOs of  $Li_6B$ ,  $Li_7B$  and  $Li_7B$ <sup>+</sup> are indeed found to be the s-orbitals that are not consistent with the energetic ordering of valence orbitals in the SJM. A fundamental difference between the PSM and SJM is that while the SJM treats the electron–electron interaction self-consistently in a positive background potential, the PSM is a one-electron approximation using confining potential. Thus in order to use the PSM, the Schrödinger equation for the one-electron-in-a-box problem needs to be solved using different box shapes.

In view of the fact that the PSM has been applied successfully for many binary clusters, a legitimate question is as to whether it can also be applied to rationalize the stability pattern of the  $Li<sub>n</sub>B$ 

<sup>\*</sup> Corresponding author. Address: Department of Chemistry, LMCC-Mathematical Modeling and Computational Science Center, Katholieke Universiteit Leuven, B-3001 Leuven, Belgium. Fax: +32 16 32 79 92.

E-mail address: [minh.nguyen@chem.kuleuven.ac.be](mailto:minh.nguyen@chem.kuleuven.ac.be) (M.T. Nguyen).

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clusters. In this work, we set out to tackle this question in carry out a theoretical investigation of electronic structure, chemical bonding and aromaticity of the species  $Li<sub>5</sub>B$  and  $Li<sub>7</sub>B$  and their isoelectronic systems  $Li_6B^+$  and  $Li_6B^-$  using quantum chemical methods. Our calculated results reveal that the electronic structure of these stable clusters is consistent with the PSM. In addition, we also probe their aromatic character.

#### 2. Computational methods

All electronic structure calculations were carried out using the GAUSSIAN 03 [23] and MOLPRO 06 [24] suites of programs. Geometry optimizations and calculations of harmonic vibrational frequencies of the clusters considered were fully performed using density functional theory with the hybrid B3LYP functional [25] and the second-order Møller–Plesset perturbation theory [26] in conjunction with the correlation consistent aug-cc-pVTZ basis set. Total electronic energies of the lowest-lying isomers were subsequently calculated using the coupled-cluster theory CCSD(T) [27], which is a more reliable method for determining the relative energies between cluster isomers.

The analysis of the chemical bonding was performed using the electron localizability indicator (ELI) [28] and the canonical molecular orbitals (MOs). Similar to the electron localization function (ELF) approach, the ELI-D scheme [29] and its orbital decomposition are proved to be an effective tool to probe the chemical bonding in organic compounds as well as in transition metal compounds [30]. The ELI is defined as the integral of the electron density over micro-cell containing the same fraction of same-spin electron pairs. It can be considered to be a product of the pair volume function and the electron density, and is equal to a sum of orbital densities in the case of single determinant wave functions. Thus, the ELI-D can be decomposed into molecular orbital contributions that are called the partial electron localizability indicator (pELI). The ELI-D values were calculated by using DGRID-4.2 program suite [31] and the ELI isosurfaces were plotted using the GOPENMOL software [32].

#### 3. Results and discussion

#### 3.1. Global minima structures

A large variety of isomeric structures for the clusters  $\rm Li_5B$ ,  $\rm Li_6B^+$ ,  $\rm Li_6B^-$  and  $\rm Li_7B$  were initially optimized using the B3LYP/aug-ccpVTZ level. Geometries of a few lowest-lying isomers were subsequently reoptimized using the MP2 and CCSD(T) methods, and their single point electronic energy calculated using the CCSD(T) method with the same aug-cc-pVTZ basis set. The optimized geometries, relative energies and number of imaginary frequencies for the lower-lying structures considered are depicted in Fig. 1, whereas their Cartesian coordinates are listed in Table S1 of the Supplementary material.

For Li<sub>5</sub>B, our findings are in good agreement with previous studies [18,20] that the high symmetry structure ( $C_{4v}$ ,  ${}^{1}A_{1}$ ) is the most stable isomer. At the B3LYP/aug-cc-pVTZ level, the two structures having  $\mathcal{C}_{\mathrm{2v}}(^{2}\mathsf{A}_{1})$  and  $\mathcal{D}_{\mathrm{3h}}(^{2}\mathsf{A}'_{1})$  point groups turn out to be transition structures having the same energetic content, and are  $\sim$ 1.5 kcal/ mol higher as compared to the global minimum.

The singlet  $O_h$  structure ( ${}^1A_{1g}$ ) is found to be the global minimum either for the anion Li $_6$ B $^-$  or for the cation Li $_6$ B $^+$ , in agreement with earlier studies. For the neutral radical  $Li<sub>7</sub>B$ , our calculated results are also consistent with previous reports [18,20] that the pentagonal bipyramid structure  $(D_{5\mathrm{h}},\ {}^1\!A_1')$  is the global equilibrium structure. The  $C_{3v}$  structure of Li<sub>7</sub>B (<sup>1</sup>A<sub>1</sub>) is found to be the second lowest-energy isomer with a relative energy of 4.3 kcal/mol (at the



Fig. 1. Shape of the optimized structures for the clusters  $Li_5B$ ,  $Li_6B^+$ ,  $Li_6B^-$  and  $Li_7B$ . Relative energies ( $\Delta E$ , kcal/mol) are obtained from CCSD(T)/aug-cc-pVTZ+ZPE calculations.

CCSD(T)/aug-cc-pVTZ level). Geometrical parameters and vibrational frequencies for the lowest-lying isomers summarized in Table 1 point out that there are small differences in geometries when using various methods. The B–Li distances in different clusters vary from 2.179 to 2.313 Å, that are close to that of the diatomic BLi  $(2.174 \text{ Å})$  [20]. The calculated stretching frequencies of the Li<sub>5</sub>B  $(C_{4v}, {}^{1}A_{1})$ ,  $Li_{6}B^{+}$   $(O_{h}, {}^{1}A_{1g})$ ,  $Li_{6}B^{-}$   $(O_{h}, {}^{1}A_{1g})$ , and  $Li_{7}B$   $(D_{5h}, {}^{1}A'_{1})$  are equal to 575, 546, 575 and 591  $cm^{-1}$ , respectively, that are quite large as compared to those of the series of  $Li<sub>n</sub>B$  clusters reported [20].

Some energetic properties of clusters were studied to measure their stability. The HOMO–LUMO gaps of the global minimum  $Li<sub>5</sub>B$  and  $Li<sub>7</sub>B$  amounts to 1.44 and 1.69 eV, respectively. The vertical ionization energy (vIE) of  $Li<sub>5</sub>B$ , which is calculated as the energy difference between the neutral  $(C_{4v}, {}^{1}A_{1})$  and the cation  $(C_{4v}, {}^{2}A_{1})$  at the neutral geometry is 4.57 eV, whereas the vIE of  $Li<sub>7</sub>B$  is 4.28 eV. As compared to the corresponding values  $\sim$  4 eV of their neighbors in the series of  $Li<sub>n</sub>B$  clusters [20], these energetic properties correlate with the fact that the neutrals  $Li<sub>5</sub>B$  and  $Li<sub>7</sub>B$  are more stable systems.

To probe the relative stability of the clusters considered, the energetic properties of clusters  $\text{Li}_n\text{B}$  ( $n = 1-8$ ) were examined in T.B. Tai, M.T. Nguyen / Chemical Physics Letters 489 (2010) 75–80 77

#### Table 1

Geometrical parameters and harmonic vibrational frequencies of global minima at B3LYP, MP2 and CCSD(T) methods with the aug-cc-pVTZ basis set.

<b>Structures</b>	$r(Li-B)$ (A)	$r(Li'-B)$ (A)	Frequencies(B3LYP) $cm^{-1}$
Li <sub>5</sub> B $(C_{4v}, {}^{1}A_1)$	$B3LYP = 2.093$ $MP2 = 2.129$ $CCSD(T) = 2.179$	$B3LYP = 2.246$ $MP2 = 2.150$ $CCSD(T) = 2.274$	575, 575, 438, 433, 432, 264, 253, 253, 196, 196, 174, 118
$Li6B+$ $(O_{h}, {}^{1}A_{1\sigma})$	$B3LYP = 2.124$ $MP2 = 2.178$ $CCSD(T) = 2.197$		546, 546, 546, 420, 415. 415, 267, 267, 267, 226, 226, 226, 178, 178, 178
Li <sub>6</sub> B $(O_{h}, {}^{1}A_{1\sigma})$	$B3LYP = 2.119$ $MP2 = 2.182$ $CCSD(T) = 2.190$		575, 575, 575, 412, 403, 403, 201, 201, 201, 200, 200, 200, 157, 157, 157
Li <sub>7</sub> B $(D_{5h}, 1A'_1)$	$B3LYP = 2.231$ $MP2 = 2.296$ $CCSD(T) = 2.313$	$B3LYP = 2.124$ $MP2 = 2.181$ $CCSD(T) = 2.195$	591, 502, 502, 406, 367. 347, 347, 270, 270, 264, 264, 219, 180, 180, 170, 170, 81, 81

term of the average binding energy  $(E_b)$ , second-order difference  $(\Delta^2 E)$  and dissociation enthalpies that are defined as follows:

$$
E_b = [nE(\text{Li}) + E(B) - E(\text{Li}_n B)]/(n+1), \tag{1}
$$

$$
\Delta^{2}E(\text{Li}_{n}B) = E(\text{Li}_{n-1}B) + E(\text{Li}_{n+1}B) - 2E(\text{Li}_{n}B). \tag{2}
$$

The plots of  $E_b$ ,  $\Delta^2 E$  and dissociation enthalpies for two dissociated channels ( $\text{Li}_n\text{B} \to \text{Li}_{n-1}\text{B} + \text{Li}$ ,  $\text{Li}_n\text{B} \to \text{Li}_n + \text{B}$ ) are depicted in Fig. 3, whereas the calculated energetic values are summarized in supporting information. It can easily be observed that the average binding energies increase with an increasing number of lithium atoms, and the highest value is attained for  $Li<sub>6</sub>B$ . The plot of second-order difference reveals two remarkable peaks at  $Li<sub>5</sub>B$  and  $Li<sub>7</sub>B$  that indicate a high stability of these clusters as compared to their neighbors. Additionally, it is fascinating to note that the dissociation enthalpy of  $Li_5B \rightarrow Li_4B + Li$  is highest as compared to corresponding values of other remains in the dissociation channel  $\text{Li}_n\text{B} \to \text{Li}_{n-1}\text{B} + \text{Li}$ . For second dissociation channel  $\text{Li}_n\text{B} \to \text{Li}_n + \text{B}$ , the highest value of dissociation enthalpy is found at the  $Li<sub>7</sub>B$ . These predictions provide a further support for our discussion about the high stability of the neutrals  $Li<sub>5</sub>B$  and  $Li<sub>7</sub>B$ .

The high symmetry cation  ${\rm Li}_6{\rm B}^+$  (O<sub>h</sub>,  $^1{\rm A}_{1{\rm g}}$ ) was reported to be highly stable species within the series of cationic clusters  $Li<sub>n</sub>B<sup>+</sup>$ [21]. According to our calculations, the HOMO–LUMO gap of  $Li<sub>6</sub>B<sup>+</sup>$  is equal to 2.43 eV (earlier value being 2.36 eV), while the vertical attachment energy (vAE) of the cation  $Li_6B^+$  that is the difference between the total energies of the cation  $\mathrm{Li}_6\mathrm{B}^+$  (O<sub>h</sub>,  $^1\mathrm{A}_{1 \mathrm{g}}$ ) and the neutral Li<sub>6</sub>B ( $O<sub>h</sub>$ ,  ${}^{2}A_{1g}$ ) at the cation optimized geometry, is 3.82 eV (previous value being 3.75 eV [21]). The anion  $Li_6B^-$  has not been reported in previous studies. Its HOMO–LUMO gap of 1.67 eV is similar to the values of 1.44 eV for  $Li<sub>5</sub>B$  and 1.69 eV for Li<sub>7</sub>B. Additionally, the global minimum of  $Li_6B^-$  is of high symmetry ( $O_{\rm h}$ ,  ${\rm ^1A_{1g}}$ ), and exhibits an electronic structure similar to that of the highly stable species  $Na<sub>6</sub>Pb$  [9].

#### 3.2. Evaluation of the aromatic character

Aromaticity is an important measure to evaluate stability of compounds. In spite of the fact that the concept of aromaticity is still not well defined, it is widely applied in the chemical literature [33]. We perform an evaluation of aromaticity of clusters by analysing the canonical molecular orbital (CMO) and the nucleus independent chemical shifts indices (NICS) indices. The NICS is based on magnetic shieldings [34], and a negative NICS value suggests an aromaticity, whereas the positive NICS values reveal an antiaromaticity and a nonaromaticity is characterized by NICS values close to zero. Because the NICS values are largely influenced by



Fig. 2. The plots of average energy, second-order difference and dissociation enthalpies of clusters  $Li<sub>n</sub>B$  (n = 2–8).

electrons in bonds, lone pairs and the core electrons [33], we consider the NICS(0), NICS(1) and NICS(2) values where the reference ghost atoms are placed at positions of 0, 1 and 2 Å above either the



**Fig. 3.** pELI-D contributions of the valence orbitals in (a)  $Li_5B$  ( $C_{4v}$ ,  ${}^{1}A_1$ ), (b)  $Li_6B^*$  ( $O_{b}$ ,  ${}^{1}A_{1g}$ ), and (c)  $Li_7B$  ( $D_{5h}$ ,  ${}^{1}A'_1$ ).

four-membered ring plane (for Li<sub>5</sub>B and Li<sub>6</sub>B<sup>+/–</sup>), or the five-membered ring plan (for  $Li<sub>7</sub>B$ ).

The MO analysis of the ground state Li $_5$ B ( $C_{\rm 4v,}$   $^1$ A $_1$ ) shows that its HOMO is a globally delocalized  $\pi$ -orbital, and the three  $\sigma$ -orbitals (HOMO-1 (degenerate) and HOMO-2) are responsible for bonding. Consequently, the neutral Li $_5$ B ( $C_{\rm 4v}$ ,  $^1$ A<sub>1</sub>) can be regarded as an  $\sigma$ -aromatic system that satisfies the Hückel rule of  $4n + 2$ electrons. NICS calculations at the B3LYP/6-311+G(d) level reveal the highly negative values (NICS(0) =  $-15.7$ , NICS(1) =  $-15.8$ , and NICS(2) = -58.2) that are consistent with high aromatic character of the species.

The NICS value of the cation  $Li_6B^+$  is also highly negative  $(NICS(1.0)$  =  $-21.1$ ,  $NICS(2.0)$  =  $-47.0$ ) that suggests a strongly aromatic structure. It is remarkable that although it possesses eight valence electrons (like its isoelectronic Li<sub>5</sub>B), the cation  $Li_6B^+$  has six globally delocalized  $\pi$ -electrons distributed over three degenerated  $\pi$ -orbitals, and that makes it a  $\pi$ -aromatic species. Following attachment of two excess electrons to the LUMO of  $\operatorname{Li_6B^+}$ , the resulting anion  $Li_6B^-$  possesses two globally delocalized  $\sigma$ -electrons and six globally delocalized  $\pi$ -electrons. Consequently, the anion  $\rm Li_6B^-$  is considered as a doubly  $\sigma$  and  $\pi$ -aromatic species in which each electron system satisfies the  $4n + 2$  electrons rule. The NICS values for the anion  $Li_6B^-$  are highly negative (NICS(1.0) =  $-27.5$ and NICS $(2.0)$  =  $-54.6$ ) that support this prediction.

For the neutral Li<sub>7</sub>B ( $D_{5h}$ , <sup>1</sup>A'<sub>1</sub>), our calculations point out that the structure is also aromatic with very highly negative NICS values  $(NICS(1.0) = -25.9; NICS(2.0) = -49.5)$ . The three orbitals (HOMO-2 (degenerate) and HOMO-3) are responsible for bond formation in the five-membered ring. While the HOMO-1 is a global  $\sigma$ -orbital, the HOMO is a global  $\pi$ -orbital. These two orbitals make the neutral  $(D_{5h}, {}^{1}A'_{1})$  doubly ( $\sigma$  and  $\pi$ ) aromatic as they contain two delocalized  $\sigma$  electrons and two delocalized  $\pi$ -electrons.

#### 3.3. Electron localizability indicator (ELI)

Another way of probing the chemical bonding and electron delocalization is to consider the electron localizability indicator (ELI). The ELI plots for structures  $Li<sub>5</sub>B$  and  $Li<sub>7</sub>B$  are depicted in Fig. 3. The localization domains of lithium (given in cyan) and boron (in light red) are mainly composed of core orbitals. The isosurfaces of p-ELI distribution for the neutral  $Li<sub>5</sub>B$  reveal that the redcolored localization domains arise from  $p_x$  and  $p_y$ -orbitals, whereas the green-colored domain is composed of  $p_z$ -orbital. Consequently, it was expected that the latter is responsible for its aromaticity. The NICS value of the neutral  $Li<sub>5</sub>B$  is increased from  $NICS(0) = -15.7$  to  $NICS(2) = -56.2$ , that is consistent with the above prediction. A similar analysis for  $Li<sub>7</sub>B$  can be obtained that the  $p_x$ - and  $p_y$ -orbitals are responsible for bond formation, whereas



Fig. 4. The energetic ordering of valence orbitals of the two-step PSM and isosurfaces (isovalues of 0.02 a.u.) of the MOs of the  $\textrm{Li}_6\textrm{B}^-$  (O $_{\textrm{h}},$   $^{1}\textrm{A}_{1 \textrm{g}}$ ).



**Fig. 5.** Isosurfaces (isovalues of 0.02 a.u.) of the MOs of the Li<sub>5</sub>B ( $C_{4v}$ ,  $^{1}A_{1}$ ) and Li<sub>7</sub>B  $(D_{5\mathrm{h}},{}^1\mathrm{A}'_1)$ . The LUMO of Li $_5$ B corresponds to the 2S shell, and the LUMO of Li $_7$ B to the 1D shell.

the added s-orbitals (their domains is not presented here) distributed as a lone pair of lithium atoms are responsible for its aromaticity.

The p-ELI plots of the cation  $Li_6B^+$  (Fig. 2b) point out that the red domains composed of three degenerate p-orbitals are distributed globally over the whole skeleton that renders the system highly aromatic. Additionally, it is obvious that there is presence of eight localized basins distributed on eight faces of the octahedral cation  $Li<sub>6</sub>B<sup>+</sup>$  that form three-center bonds, and give a support for the high stability of this structure. There is negligible difference between the p-ELI plots of  $Li<sub>6</sub>B$  in both cationic and anionic states. Similar to the case of Li<sub>7</sub>B, added s-orbital (HOMO) of the anion  $Li_6B^$ was delocalized as a lone pair of lithium atoms and contribute to the enhanced aromaticity of the anion  $Li_6B^-$ .

#### 3.4. Phenomenological shell model (PSM)

We now rationalize the electronic structure of the clusters Li<sub>5</sub>B.  $Li_6B^+$ ,  $Li_6B^-$  and  $Li_7B$  within the framework of the PSM. The energetic ordering of the valence molecular orbitals of the  $Li_6B^-$  anion in conjunction with the ordering of the model is shown in Fig. 4. Similar correlations for the clusters  $Li<sub>5</sub>B$  and  $Li<sub>7</sub>B$  are depicted in Fig. 5. The three higher-lying orbitals (HOMO and degenerate HOMO-1) show a p-character, whereas the HOMO-2 is an s-orbital. The LUMO of  $Li<sub>5</sub>B$  turns out to be an s orbital, and contributes predominantly to the 2S shell orbital. As a consequence, the neutral Li<sub>5</sub>B is consistent with the configuration  $(1S^2 \t1P^6)$  of the PSM. A similar observation was found for the cation  $Li_6B^+$  in which the three degenerate p-orbitals and one s-orbital (HOMO-1) are fully occupied by eight valence electrons, whereas its LUMO is an s-orbital, and contributes to the 2S shell orbital. This distribution is again consistent with the PSM configuration of  $(1S<sup>2</sup> 1P<sup>6</sup>)$ .

For systems of 10 valence electrons including  $Li_6B^-$  and  $Li_7B$ , addition of one B atom that is a more electronegative element as compared to lithium results in a perturbation of the energy ordering of the valence orbitals taking part in the PSM. Thus, the systems possessing 10 valence electrons can be accounted for with the PSM configuration of ( $1S^2 1P^6 2S^2$ ). Fig. 5 shows that the neutral Li<sub>7</sub>B has 10 valence electrons and they are in line with the PSM arrangement. Its HOMO and HOMO-3 are two s-orbitals, whereas its HOMO $-1$  can be regarded as a p<sub>z</sub>-orbital and the degenerate orbital HOMO–2 is  $\bm{{\mathsf{p}}}_{{\mathsf{x}}}$  and  $\bm{{\mathsf{p}}}_{{\mathsf{y}}}$ -orbitals. A similar picture is also observed for the anion  $Li<sub>6</sub>B<sup>-</sup>$  in which the two excess electrons occupy the sorbitals leading to the PSM configuration of  $(1S<sup>2</sup> 1P<sup>6</sup> 2S<sup>2</sup>)$ .

#### 4. Conclusion

In this present theoretical study, we determined the geometries of the boron-doped clusters  $Li_5B$ ,  $Li_6B^+$  and  $Li_6B^-$  and  $Li_7B$  using the B3LYP and MP2 methods. The global minima for clusters were found and further confirmed by coupled-cluster theory CCSD(T) calculations. These clusters have large vertical ionization energies, large HOMO–LUMO gaps and high degree of aromaticity as compared to the other members of the series of clusters  $Li<sub>n</sub>B$ . In particular, we have demonstrated that the electronic structure of these species, and thereby their high stability, can perfectly be accounted for by the phenomenological shell model.

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#### Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at [doi:10.1016/j.cplett.2010.02.036](http://dx.doi.org/10.1016/j.cplett.2010.02.036).

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